FX Intervention, Reserves Accumulation, and Financial Intermediation

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FX Intervention and Reserves

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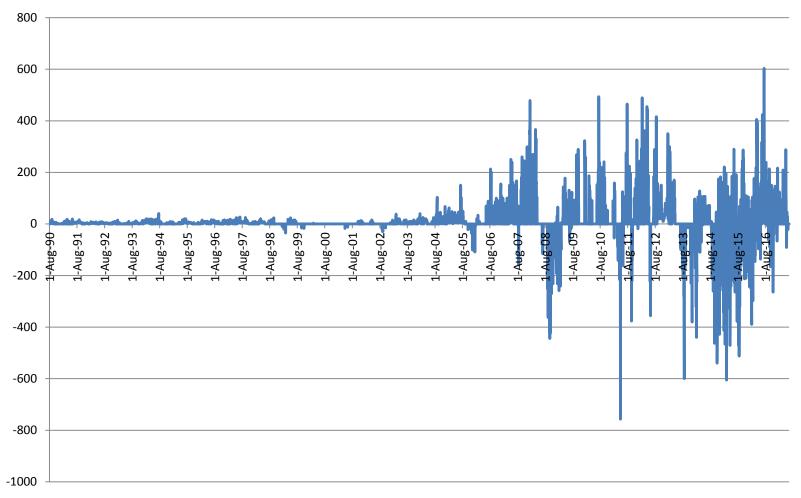
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Two recent trends:

Intervention State Action Foreign Exchange Intervention

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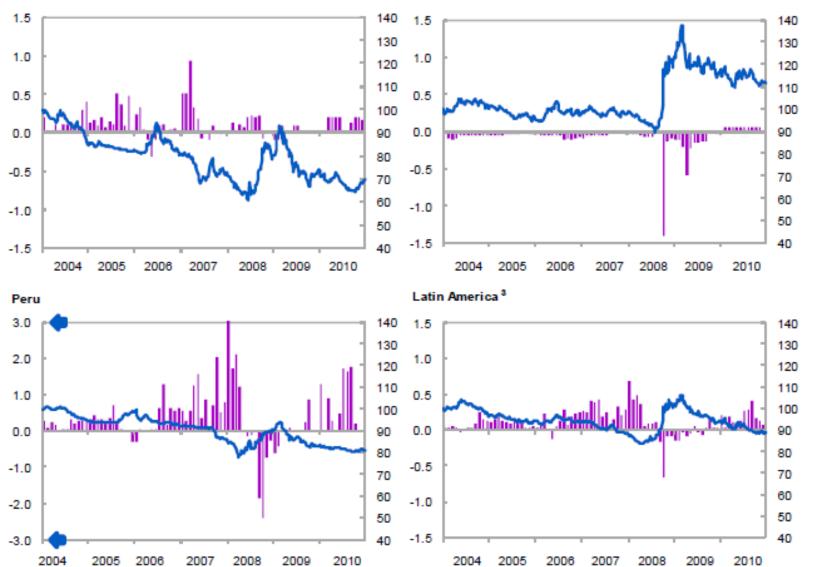
- Foreign Exchange Intervention
- 2 Reserves Accumulation



Peru: FX Intervention (Daily, US\$ Millions)

Source: Central Bank of Peru

Colombia



Mexico²

Left axis: FX Intervention, Percent of GDP; Right axis: Exchange Rate **Source**: Adler and Tovar (2011)

	Frequency (Percent of working days)	Intensity			
		Cumulative intervention as percent of GDP ^{1,2}	•	Daily maximum (Millions of U.S. dollars) ¹	Has there been active FX intervention in 2011?
Chile	6	3.8	50	50	yes
Colombia	32	10.3	34	733	yes
Guatemala	19	1.6	9	332	yes
Mexico ³	1	0.6	600	600	yes
Peru	39	36.1	55	494	yes
Latin America ⁴ Others	19	10.5	150	442	
Australia ⁵	62	2.5	15	377	n.a.
Israel	24	22.3	84	300	no ⁶
Turkey	66	12.5	61	4966	yes

Table 1. Stylized Facts of Foreign Exchange Purchases, 2004–10

Source: Adler and Tovar (2011)

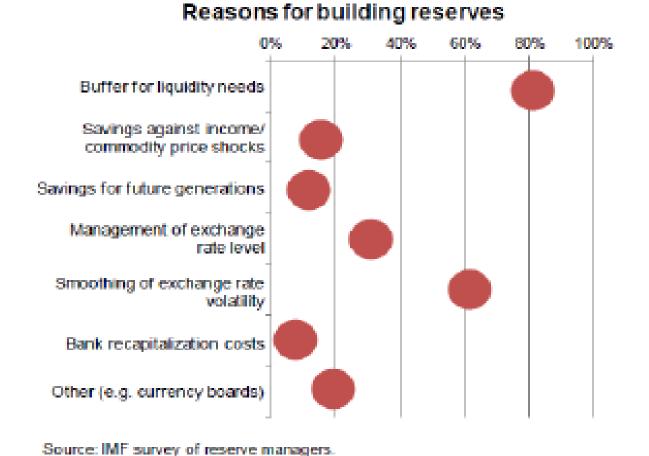
Foreign exchange reserves and exchange rates



Left axis: US\$ per domestic currency. Right axis: US\$ billion **Source**: Chutasripanish and Yetman (2015)



Source : Irina Bunda (2016)



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- What are the determinants of optimal reserves?
- What are the costs and benefits of reserves?

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- In the model, external constraints can become binding endogenously and result in a credit crunch
- International reserves enable the central bank to provide international liquidity and alleviate financial constraints when they bind
- The optimal level of reserves is tightly linked to the impact and nature of *ex post* intervention

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- Optimal reserves depend on nature and degree of financial frictions and financial development
- And on the specific policies that the central bank can use in the event of a liquidity crunch
- An increase in *ex ante* uncertainty also justifies a buildup of reserves

• Recent work on fx intervention and "unconventional" monetary policy: Chang (2018), Céspedes-Chang-Velasco (2018)

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- Optimal Reserves: Jeanne-Korinek

A Basic Model

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• t = 0, 1, 2

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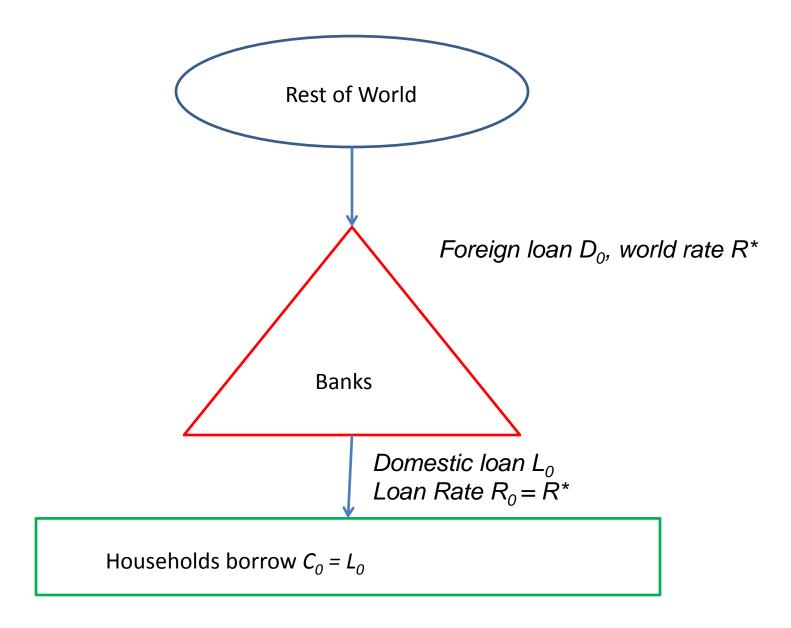
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- Small open economy

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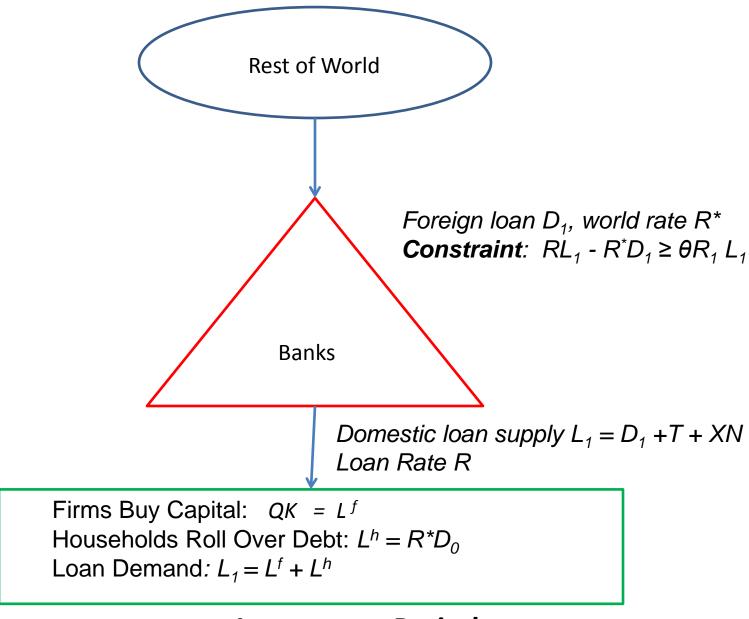
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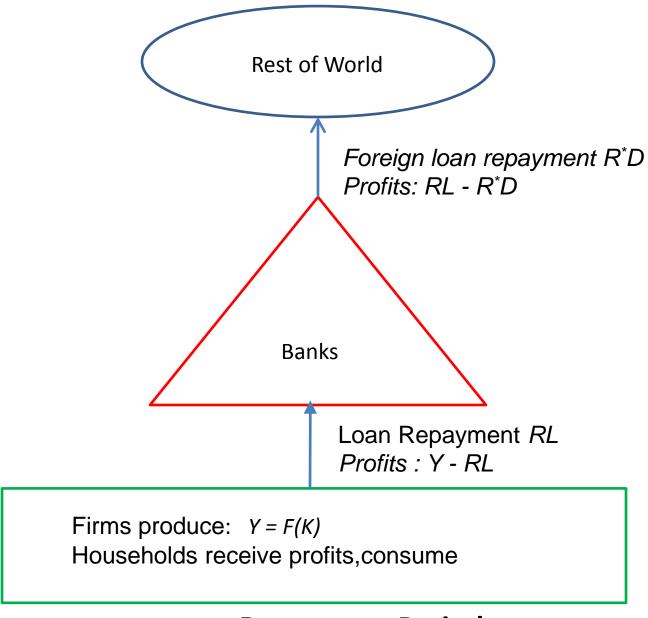
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- Financial intermediation subject to frictions and shocks



Initial Period



Investment Period



Repayment Period

Households consume only tradables and have preferences

 $u(C_0) + \beta EC_2$

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- t = 1: they roll over their debt, and hence $L_1^h = R_0^* L_0^h$ • t = 2:

$$C_2 = \Pi^b + \Pi^f - R_1 L_1^h$$

= $\Pi^b + \Pi^f - R_1 R_0^* C_0$

Initial consumption (and debt) are then given by the first order condition:

$$u'(C_0) = \beta R_0^* E R_1$$

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==> Note that if $ER_1 > R_1^*$, borrowing is inefficiently low

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• Demand for capital is then given by:

$$\alpha A K_2^{\alpha-1} = R_1 Q_1$$

Capital is an aggregate of tradables and nontradables:

$$K_2 = \kappa I_{h1}^{\gamma} I_{w1}^{1-\gamma}$$

Image: A math a math

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• In equilibrium $I_{h1} = N$, so K_2 and Q_1 are pinned down by X_1



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• t = 2: Bank profits are

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- Similar to CCV (2018) and others
- Departure: heta is a **random variable** realized at t=1
- This is the only source of uncertainty (for now, at least)

Laissez Faire Equilibrium

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Consider the economy from t = 1 on:

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where X_{1f} is the **frictionless** exchange rate • If $R_1 > R_1^*$, the bank borrows as much as it can, and lends

$$L_1 = \frac{1}{1 - (1 - \theta)\phi} (T + X_1 N)$$

where $\phi = R_1/R_1^*$ is the interest rate spread.

If financial constraints do **not** bind, $R_1 = R_1^*$, and all other variables take their frictionless (**f**) values:

$$\alpha A K_{2f}^{\alpha-1} = R_1^* Q_{1f} = R_1^* X_{1f}^{\gamma}$$
$$\frac{X_{1f} N}{I_{wf}} = \frac{\gamma}{1-\gamma}$$
$$K_{2f} = \kappa N^{\gamma} I_{wf}^{1-\gamma}$$

Hence the collateral constraint will not bind in the continuation if:

$$L_1 = R_0^* C_0 + Q_{1f} K_{2f} \le \frac{1}{\theta} (T + X_{1f} N)$$

i.e. if $\theta \leq \hat{\theta}$, where

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- Note that $\hat{ heta}$ is endogenous and, in particular, falls with C_0

If $\theta \leq \hat{\theta}$, then $R_1 > R_1^*$ and relative prices adjust to clear markets. In particular, the equilibrium exchange rate solves:

$$R_0^* C_0 + Q_1 K_2 = \frac{1}{1 - (1 - \theta)\phi} (T + X_1 N)$$

where the spread ϕ is given by

$$\phi = R_1 / R_1^* = \left(\frac{X_f}{X_1}\right)^{\gamma + (1-\alpha)(1-\gamma)}$$

Initial Debt

Recall that, in any continuation equilibrium

$$\begin{array}{rcl} {\cal R}_1 & = & {\cal R}_1^* \text{ if } \theta \leq \hat{\theta} \\ & = & \rho({\cal C}_0, \theta) & \text{if } \theta > \hat{\theta} \end{array}$$

The Euler equation

$$u'(C_0) = \beta R_0^* E R_1$$

becomes

$$u'(C_0) = \beta R_0^* \left[R_1^* F(\hat{\theta}) + \int_{\hat{\theta}}^{\bar{\theta}} \rho(C_0, \theta) F(d\theta) \right]$$

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- This equation yields C_0
- (Note that $\hat{\theta}$ depends on C_0)

Some Implications

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- Some determinants are the "obvious" ones: i.e. lower productivity (lower A) lead to lower $\hat{\theta}$ and higher probability of crises
- Other ones are novel
- Most interesting: an increase in uncertainty (a mean preserving spread in θ) can lead to higher crises probability

• Consider a planner that sets only initial consumption and debt, $C_0 = D_0 = L_0$, and leaves the rest of the economy to subsequently adjust to equilibrium.

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- The planner would then maximize $u(C_0) + \beta EC_2$ subject to the laissez faire equilibrium conditions, except the Euler equation

The solution to the planner's problem can be written as:

$$U'(C_0) - \beta R_1^* R_0^* = \beta R_0^* E\left\{ (R_1 - R_1^*) E I_D^X \frac{I_w}{R_0^* C_0} \right\}$$

where $El_D^X = -\frac{C_0 dX_1}{X_1 dC_0} \ge 0$ is the elasticity of the xrate X_1 wrt initial debt $D_0 = C_0$

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- The RHS is the cost, which is expressed by the spread (divergence between marginal benefit of tradables investment and world interest rate)

Forex Reserves and Intervention

• Suppose now that, at t = 0, the central bank can borrow tradables in the world market.

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- The central bank can invest F in the world market and earn R_0^* or R_1^* .

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- The central bank can invest F in the world market and earn R_0^* or R_1^* .
- But in period t = 1 it also has the option to use F to enact policies aimed at alleviating financial frictions, if these turn out to be binding.

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==> The answers depend on the policies that the central bank implements in t = 1.

• Baseline: at t = 1, the central provides a loan of size F to domestic banks when financial constraints bind.

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- In terms of Gertler-Kiyotaki (2010), the central bank provides "liquidity facilities ".
- CCV (2018): this is equivalent to other interesting policies, and more effective than providing loans to households or firms, in particular.

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loan supply is now constrained by

$$L_1 \leq \frac{1}{1 - (1 - \theta)\phi} (T + X_1 N + F)$$

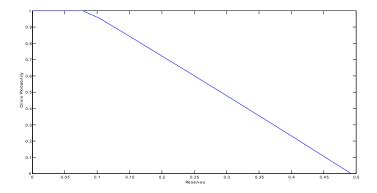
Theorem

If the term premium $\tau = 0$, F will be large enough to drive the probability of crises to zero. If $\tau > 0$, however, it is not optimal to eliminate crises completely.

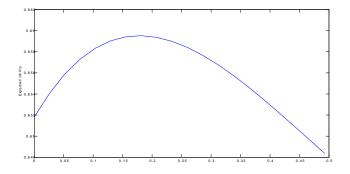
• If au = 0, holding reserves has no opportunity cost

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- The marginal gain to eliminating crises completely is of second order, so it is not optimal to do that if $\tau > 0$

Numerical Illustrations



Large enough reserves can eliminate crises completely...

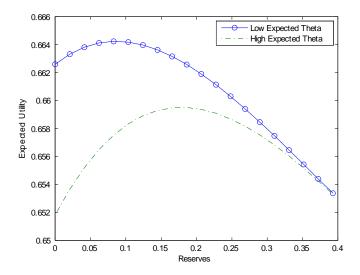


...but it is not optimal, if term premium is positive

$\bullet\,$ Consider a fall in the mean value of $\theta\,$

- Consider a fall in the mean value of heta
- This captures differences in financial development

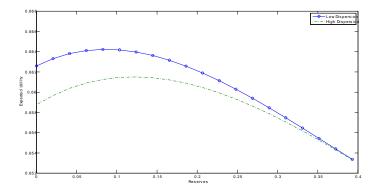
- Consider a fall in the mean value of heta
- This captures differences in financial development
- Correspondingly, one would expect that optimal reserves should be smaller



Reserves and Expected Utility with $\theta = 0.38$ and $\theta = 0.4$

• A mean preserving spread of θ leads to higher reserves

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- This is in line with intuition, and with observed experiences

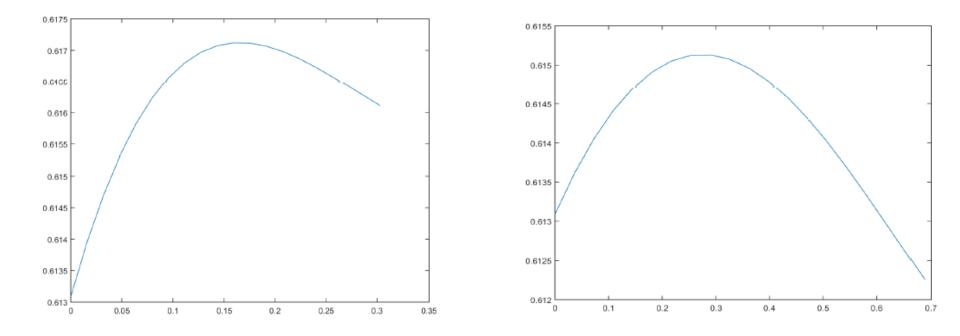


Uncertainty and Optimal Reserves

• As in CCV, the central bank uses reserves more effectively if it lends them to banks instead of firms or households in a credit crunch

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- But direct lending may be more feasible because of other reasons (e.g. political)
- With direct lending, optimal reserves must be larger



FX Reserves and Mode of Intervention: Left: Equity Injections Right: Direct Lending

Final Remarks

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- Thank you!!